In the Final Analysis

The 2006 L S Theobald Lecture

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The three essentials of quality

- What accuracy does the customer <u>NEED</u>? Fitness for purpose (Decision theory)
- What accuracy <u>CAN</u> I achieve? Single laboratory validation Collaborative trials
- What accuracy <u>DO</u> I achieve? Internal quality control Proficiency testing

Three issues relating to quality

- Fitness for purpose (What is it?)
- Statistics (Can we do it?)
- Metrology (Do we need it?)

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Using simple statistics for x_a and $z = (x - \overline{x})/s$





88% of z-scores within the range -2<z



	$\mathbf{x}^{\mathrm{T}} = \begin{bmatrix} x_1 & x_2 & \cdots & x_n \end{bmatrix}$
Set $1 < k < 2$, $p = 0$, $\hat{\mu}_0$ = median, $\hat{\sigma}_0 = 1.5 \times \text{MAD}$	
	$x_i \qquad p-k_p < x_i < \mu_p + k\sigma_p$ $x_i = \mu_p - k\sigma_p \qquad x_i < \mu_p - k\sigma_p$ $\mu_p + k\sigma_p \qquad x_i < \mu_p + k\sigma_p$



 \overline{r}



 $\overline{=}$





















The normal kernel density

$$y = \frac{1}{nh} \sum_{i=1}^{n} \Phi \ \frac{x - x_i}{h}$$
where is the standard normal density,

$$\Phi(a) = \frac{\exp(-a^2/2)}{\sqrt{2\pi}}$$
AMC Technical Brief No. 4











The normal mixture model

$$f(y) = \sum_{j=1}^{m} p_j f_j(y), \quad \sum_{j=1}^{m} p_j = 1$$

$$f_j(y) = \frac{\exp(-(y - \mu_j)^2 / 2\sigma^2)}{\sqrt{2\pi\sigma}}$$
AMC Technical Brief No 23, and AMC Software.
Thompson, Acc Qual Assur, 2006, **10**, 501-505.

Mixture models found by the maximum
likelihood method (the EM algorithm)
• The M-step

$$\hat{p}_{-j} = \sum_{i=1}^{n} \hat{P}(j|y_i) / n$$

 $\hat{\mu}_j = \sum_{i=1}^{n} y_i \hat{P}(j|y_i) / \sum_{i=1}^{n} \hat{P}(j|y_i)$
 $\hat{\sigma}^2 = \sum_{j=l=i}^{n} \sum_{i=1}^{m} ((y_i - \hat{\mu}_j)^2 \hat{P}(j|y_i)) / \hat{P}(j|y_i)$
• The E-step
 $\hat{P}(j|y_i) = \hat{p}_j f_j(y_i) / \sum_{i=1}^{m} \hat{p}_j f_j(y_i)$





Find out more?

AMC Technical Briefs and Software on www.rsc.org/amc/

Statistics

• Lies, damned lies, and statistics!

Metrology

• Fiction, science fiction, and metrology!

Metrologist's creed

- Uncertainty is important.
- Analytical chemists are not good at estimating uncertainty.
- All results of chemical measurement are traceable to SI units, in particular the mole, the kilogramme, the metre.
- Analytical chemists don't worry about traceability, that's why their results are questionable.

Metrological false premise 1

- All analytical results are traceable to SI units, in particular the mole, the kilogramme, and the metre.
- *NO!* The majority of analytical measuremnts made for commercial purposes are mass fractions, not traceable to *any* unit. *Corollory:* expressions such as %, ppm, ppb, etc are perfectly correct.





False premise No 1 contd. – Silly or what!

- Is the concentration of silver, A/B, traceable to the metre ?
- Should we express the result as (say) 70 cm m⁻¹?
- Or 700 mg g⁻¹ (when no mass standard is involved)?

Metrological false premise 2

- Chemical measurement results are not accurate enough, and that is because of a lack of traceability to SI units.
- NO! Most chemical measurement results are fit for purpose or more accurate.
- Where results are not accurate enough—it sometimes happens—the shortfall is often irreducible and traceability to SI units does not help.





Reproducibility relative standard deviations







Metrological false premise 4

- Chemical measurements have a larger relative uncertainty in comparison with most physical measurements. (True)
- That is because they are not traceable to SI units.
- *NO!* The traceability chain to SI units contributes almost nothing to the combined uncertainty of analytical results.

Metrological false premise 4 contd.

- Realistic relative uncertainties in analytical results are mostly in the approximate range 1-30%.
- Relative uncertainties in tranferring SI units (such as mass and volume) to the analytical laboratory bench are less than 0.1%.

Metrological false premise 5

- Terms such as "true value", "trueness", and "bias" have no proper place in metrology (because we can't know them).
- *NO!* "True value" (and its dependent terms) are readily defined.
- The whole of statistics is based on the idea of unknown population values, a concept logically isomorphic with "true value".

Metrological false premise 6

- Only accredited laboratories can produce reliable results.
- <u>Nol</u> Evidence from proficiency tests contradicts this idea.

Metrological false premise 6



